

Heat Transfer Investigation in an Engine Exhaust-Type Pulsating Flow

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Abstract - In many practical engineering situations, such as in the exhaust pipes of Internal Combustion Engines, heat is transferred under conditions of pulsating flow. In these conditions, the heat transfer mechanism is affected by the pulsating flow parameters. The objective of the present work was to experimentally investigate heat transfers for pulsatile turbulent flows in a pipe. A specific experimental apparatus able to reproduce a pulsating flow representative of the engine exhaust was designed. A stationary turbulent hot air flow with a Reynolds number ranging from 1.8×10^4 to 3.5×10^4 , based on the time averaged velocity, is excited through a pulsating mechanism and exchanges thermal energy with a steel pipe. Pulsation frequency ranges from 10 to 95 Hz. The effects of pulsation frequency and pipe length on the convective heat transfer were evaluated. It was observed that flow pulsation enhances convective heat transfers in comparison with the steady case. The results highlight that, when the flow is excited with a pulsation frequency equal to a resonance mode of the system, a local maximum of the heat transfer rate appears. This behaviour was found to be independent of the pipe length. Instantaneous measurements of air velocity and temperature demonstrated that the increase in the energy axial advection due to the oscillating component of the velocity is the major cause of the heat transfer enhancement.

Keywords: Convective Heat Transfer Enhancement, Pulsating Flow, Internal Combustion Engine, Waste Heat Recovery.

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1. Introduction

Legislation on vehicle emissions continues to become ever more stringent in an effort to minimize the impact of Internal Combustion Engines (ICEs) on the environment, constraining engine manufacturers to face the challenge of increasing engine efficiency and decreasing pollutant emissions. ICE efficiency is still improving but it is today limited at best to around 40%, as a large part of the energy contained in the fuel is lost in coolant, oil, exhaust gas and air around the engine. Considering the exergetic limits, Waste Energy Recovery (WER) is a promising way to go further in fuel saving and pollutant emission control: a waste heat recovery system produces power by using the heat energy available at the exhaust, without additional fuel input. Besides the use of WER to increase ICE efficiency, particular attention is also being paid to the design of catalytic converters and exhaust manifold to comply with emission standards requirements. In order to reduce emission during the cold start phase, various solutions can be implemented in both the engine and exhaust system, such as a faster catalytic converter action to increase the efficiency of exhaust gas processing. Among all the techniques proposed in the past few years, as demonstrated by the work of Petković et al. [1], passive systems are being widely investigated. They include a simple constructional alteration on the exhaust manifold, which can be used to reduce heat losses to the atmosphere. For WER systems as well as for the design of engine exhausts, good management of the heat transfer phenomena is an important requirement, as demonstrated by the work of Host et al. [2]. Heat transfers in engine manifolds occur under pulsating conditions. The term 'pulsating' is used

for cycle-stationary flows in which the oscillations occur around a time-averaged value different from zero. Although for a stationary flow the Reynolds number characterizes the laminar or turbulent behaviour of the bulk flow, the amplitude and the frequency of the superimposed oscillations play a dominant role in the structures of the pulsating flow. In recent decades, extensive studies have been dedicated to pulsating flows, and their associated heat transfer process, in a wide range of experimental configurations. However, some available results are contradictory and the main questions are still open: does pulsation enhance or else degrade heat transfers compared to a steady flow? What are the main heat transfer mechanisms?

2. Related Work

Dec et al. [3], [4] studied the influence of pulsation frequency (f), amplitude and mean flow rate on the heat transfers for a pulse combustor tail pipe. Pulsation frequency was varied from 67 to 100 Hz, for a Reynolds number (Re) based on the time-averaged velocity varying between 3100 and 4750. Several mechanisms responsible for the heat transfer enhancement in reversing, oscillating turbulent flows were presented and discussed, among which acoustic streaming, entrance effects and the turbulence intensity increase. According to the authors, the influence of both acoustic streaming (which corresponds to the appearance of a secondary time-averaged velocity component having the form of large longitudinal recirculation cells) and entrance effects on the observed Nusselt number (Nu) enhancement was small. In further studies, time-resolved velocities [5] and temperatures [6] were analysed to describe the heat transfer enhancement mechanism. The results suggested that a combination of increased shear-layer generated turbulence and strong convection at the zero-velocity crossings by transverse flows was the most plausible explanation for the mechanism causing the observed heat transfer enhancement. Xu et al. [7] studied the flow properties of a self-excited Helmholtz pulse combustor elbow tailpipe. The results showed that, due to pulsation and flow reversal, Dean Vortex forming, shedding and reforming process periodically contribute to convective heat transfer enhancement. With the same type of experimental apparatus, Zhai et al. [8] proposed a Nusselt correlation for the pulsating flow, based on the addition of two independent physical properties. Applying the quasi-steady theory and the Vaschy-Buckingham theorem to the convection heat

transfer problem, the ratio between the velocity amplitude and the time-averaged velocity and the ratio between the pulsation velocity scale and the time-averaged velocity were found to be the aforementioned independent physical properties. Several studies were also conducted on turbulent and laminar pulsating pipe flows. In the work of Patel et al. [9], the Reynolds number ranged from 7000 to 16500, while the pulsation frequency was varied from 1 Hz to 3.33 Hz. Results showed that the Nusselt number was strongly affected by both pulsation frequency and Reynolds number with a 44.4% maximum enhancement of the heat transfer coefficient at the pulsation frequency of 3.33 Hz. In a study on a pulsating turbulent water stream, Zohir [10] also pointed out that the heat transfer coefficient was strongly affected by pulsation frequency and amplitude and by the Reynolds number. The improvement in heat transfers was attributed to an increased level of turbulence and the introduction of forced convection in the boundary layer. In the study by Li et al. [11] on heat transfer in turbulent pulsating pipe flows, the time-averaged Reynolds number varied from 6×10^4 to 12×10^4 and pulsation frequency ranged from 0 to 100 Hz. Results showed that the Nusselt number was improved with the increase in the Reynolds number and the pulsation amplitude, defined as the ratio between the pressure amplitudes at the inlet and outlet of the pipe. Otherwise, the Nusselt number decreased with the increase in the Womersley number (Wo) up to a value of $Wo=130$, but a maximum value was obtained for a pulsation frequency of 90Hz approximately, corresponding to $Wo=150$. Habib et al. [12] studied the heat transfers in laminar pulsating pipe flows, where the Reynolds number and the pulsation frequency ranged from 780 to 1987, and from 1 to 29.5 Hz respectively. The results showed that the pulsation frequency affected heat transfers stronger than the Reynolds number. Compared to a steady flow, both an enhancement and a reduction of heat transfers, corresponding to different pulsation frequency ranges, were observed. In turbulent conditions (for a Reynolds numbers range of 5000 – 29000), Habib et al. [13] also found an increase or a decrease of heat transfer as a function of the pulsation frequency. The turbulent bursting mode was identified as a possible explanation for the observed heat transfer modification. Likewise, in the work of Monschandreou et al. [14], both an enhancement and a degradation of heat transfers was observed: the results indicated that, in a range of moderate frequency values, the effect of the pulsation

was to increase the bulk temperature of the fluid and the Nusselt number, but the effect was reversed outside this range. The experimental studies by Said et al. [15] and Nishandar et al. [16] confirmed that the heat transfer coefficient was either increased or decreased function of the pulsation frequency in turbulent conditions. Elshafei et al. [17] studied numerically conducted a numerical study of the heat transfers for a fully developed pulsating turbulent flow over a range of $10^4 \leq Re \leq 4 \times 10^4$ and $0 \leq f \leq 70$ Hz and the results were compared with the available experimental data. Results showed a slight reduction in the time-averaged Nusselt number with respect to that of a steady flow. However, in the fully developed established region, the local Nusselt number was either increased or decreased, compared to Nu values for steady flow, depending on the frequency parameter. As reported by the aforementioned surveys, it has been frequently observed that pulsation frequency may have an impact on the convective heat transfers. However, the variety of the experimental configurations and the variety of the pulsation creation mechanisms have led to some controversies: both enhancement and degradation of convective heat transfers have been observed. Besides, the main physical mechanisms involved have not been fully described. In the present study, an experimental investigation was conducted on heat transfer phenomena for a pulsating turbulent pipe flow, in a wide range of variation of the physical parameters. The main purposes were to investigate the impact of the pulsation frequency on heat transfers and to identify the main physical mechanisms involved in the heat transfer modification. Particular attention was paid to the calculation of the time-averaged convective heat transfer by developing an analytical formulation of the heat transfer problem. The design of an experimental apparatus, able to reproduce a pulsating pipe hot air flow over a range of $10 \leq f \leq 95$ Hz and $1.8 \times 10^4 \leq Re \leq 3.5 \times 10^4$, representative of engine exhaust flow operating conditions, is presented. In the test-rig, the pulsating hot air flow exchanges thermal energy with cold water flowing in the opposite direction. The work presented in this paper focuses only on the time- and space-averaged characterization of the convective heat transfers, using a 1D flow hypothesis. Data collection and reduction are presented; results are reported and discussed based on this assumption.

3. Experimental Setup and Procedures

3. 1. Experimental Setup

A schematic diagram of the pulsatile flow facility is depicted in figure 1. It comprises three main parts: the first one produces a hot stationary air flow, the second one transforms the stationary flow to a pulsating flow, and in the last part, in which the flow develops, heat transfers are estimated. In the first part of the test rig, the dry compressed air mass flow rate is measured and regulated by a Brooks SLA5853S {1}, a thermal effect mass flow meter with a maximum flow rate of 2500 NI/min and with a calibration uncertainty of 0.73% of full scale. Then, air is heated by three Sylvania inline air heaters {3} with a total electric power of 12 kW, ensuring a maximum air temperature of 400°C at the maximum mass flow rate. Hot flow is finally stored in a 30-litre steel tank {4} designed to withstand a maximum air pressure of 10 bar and to dampen the flow pulsation coming back from the pulse generator. Once the hot air flow has been generated it is forced to pass through the pulsating mechanism {5-7}: a mono-cylinder head was chosen to produce a pulsating flow with a maximum frequency of 95 Hz, equipped with a classical pushrod valve train entrained by an electric engine with a power of 3 kW and a nominal velocity of 3000 rpm. In detail, hot air flows from the bottom of the cylinder head and only one of the two intake valves is alternately closed and opened to create the pulsating flow. The intake valve was chosen because of its higher diameter. Air leakages in the cylinder head were experimentally estimated to be below 0.5 kg/h, leading to an error on the mass flow rate measurement of <1%. In order to determine the camshaft position and rotation velocity, an encoder with a resolution of 0.1° is placed on the camshaft. Once the pulsating flow is generated, it is forced to pass through a steel pipe {8-10} in which it develops and exchanges thermal energy. Finally, at the end of the pipe, a 6-litre tank {11} is placed to muffle pressure pulsations. The entire flow facility is then linked to the exhaust line of the laboratory. As shown in figure 1, the steel pipe is composed of three different sections: the first one, called *developing section* {8}, has a length of 2.65 meters and a pipe length/internal diameter ratio of 48.4. It was designed to be long enough to completely develop the velocity flow field in the case of a steady turbulent flow.

The pipe is thermally insulated to avoid high heat energy losses. The test section {9} (detailed in figure 2), with a length of 1 meter, is placed at the outlet of the

developing section and is designed to be able to characterize heat transfers.

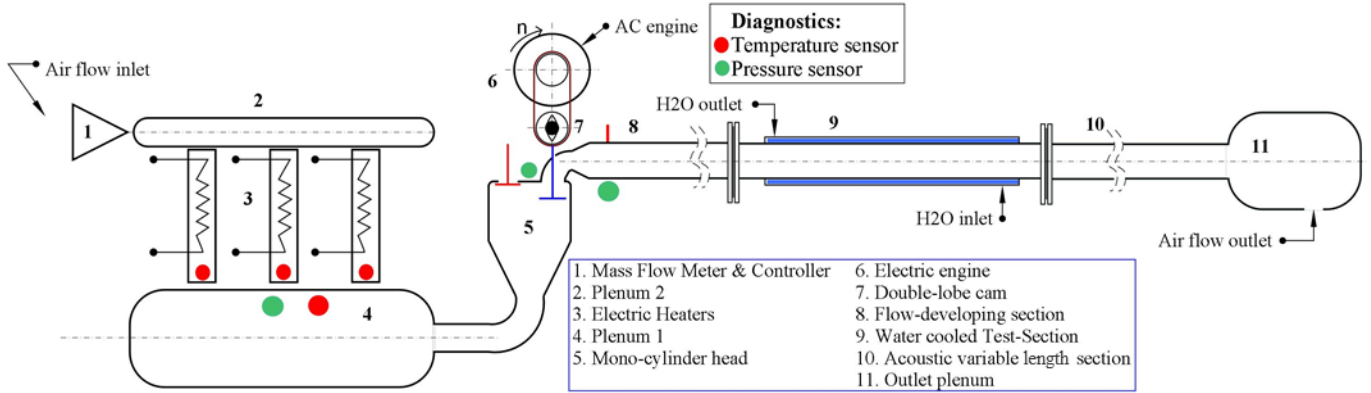


Figure 1. Scheme of the Experimental Apparatus.

The test section consists of a double-wall pipe, in which the pulsating air and cold water flow in opposite directions, respectively in the internal and external parts of the pipe. Water cooling has the advantage of making it possible to manage the wall temperature and of having a homogeneous temperature field in the internal wall of the pipe. Inlet and outlet water temperatures are measured by two 0.5 mm sheathed K-type thermocouples in order to evaluate the total time-averaged convective heat transfer Q_{conv} (see Eq. 7). A Kistler Type 2621F conditioning unit, with a maximum cooling power up to 1500 Watt, is used to provide a maximum water flow rate of 6.1 l/min. As shown in figure 2, at a distance from the beginning of the test-section of 10 times the internal pipe diameter, several sensors are placed to measure the air velocity, temperature and pressure. In particular, in order to calculate the air bulk temperature, which corresponds to the integral of temperature on the cross section, in the first measuring section (A - A' in figure 2) four sheathed K-type thermocouples with a 0.5 mm diameter are placed at different distances from the wall, respectively 1, 0.5, 0.125 and 0.0625 times the pipe radius. Furthermore, a Kulite pressure transducer is placed to measure the instantaneous static pressure of air. The same measuring configuration was used for the outlet section of the test-section. For the remaining sections, except the section B - B', only one 0.5 mm sheathed K-type thermocouple is placed at the centreline of the pipe. In the section B - B', in addition to a Kulite pressure transducer, a Constant Temperature Anemometer and two unsheathed micro-thermocouples are placed to measure the instantaneous

radial profiles of air velocity and temperature. In particular, a Dantec 55P71 double wire probe (HWA in figure 2) was used to measure the air velocity magnitude and to detect flow reversal. The energy balance equation applied to the hot junction of a thermocouple describes the temperature difference between the gas and the hot junction with a thermocouple temperature delay due to the finite mass of the hot junction and due to the convective heat transfer between the fluid and the thermocouple. Assuming negligible thermal conduction and radiation in this equation, the hot junction temperature can be modelled as a first-order system, where the time constant represents the requested time the sensor needs to reach the gas temperature. For rapid temperature measurements, such time constant has to be compared to the dynamic of the flow properties variation in order to know if a compensation of the time delay has to be applied to the thermocouple signal to compute the real fluid temperature. A Kalman Filter method [18] was applied to the signal of the two micro-thermocouples (T1-kf, T2-kf in figure 2) to calculate in-situ the time constant of the sensor in order to correct the raw thermocouple measurements and to estimate the actual air temperature. The method has been experimentally validated using a reference temperature signal measured with a cold wire with a diameter of 1 μm which has a frequency bandwidth up to 1 kHz. An uncertainty less than 3% has been found. The HWA and the micro-thermocouples are connected to the pipe with a concentric screw system with a thread pitch of 1 mm. As shown in figure 1, downstream the test-section, a pipe with a variable length was used. The total length

of the pipe can vary from 3.61 meters to 5.91 meters. A NI-9035 cRIO and the LabView software were used to control all the devices in the experimental apparatus and to acquire data.

3.2. Procedure

The study of the impact of the flow pulsation on heat transfer phenomena is achieved by exciting a steady hot air flow with a pulsation frequency ranging from 0 to 95 Hz. The minimum attainable frequency is 10 Hz; for lower frequencies the electric motor is

unable to perform constant speed revolution. A time-averaged mass flow rate varies from 90 to 130 kg/h and is forced to flow through the mono-cylinder head. The centreline air temperature at the inlet of the test-section is maintained constant at 150°C for all experiments by regulating the electric power of the air heaters with a PID controller. These flow conditions correspond to a time-averaged Reynolds number varying from 19000 to 35000, corresponding to turbulent flow state conditions.

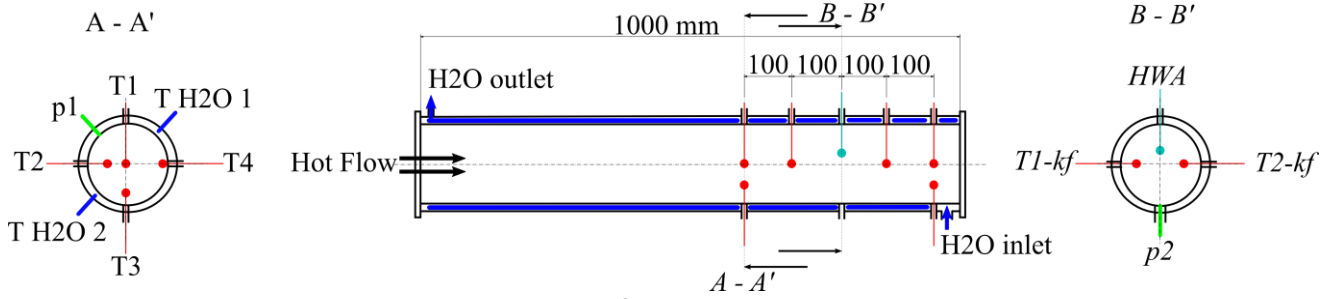


Figure 2. Test-section.

The cooling water temperature at the inlet of the test-section is kept constant at 17.4°C for each experiment, with a maximum test-by-test variation of around 0.2°C.

The instantaneous mass flow rate profile imposed on the flow, in this manner, is dependent on the flow pulsation frequency and the pipe acoustic responses. This means that while the time-averaged component of the mass flow rate is kept constant for all the flow pulsations, the oscillating component is not constant. In order to extract coherent phenomena responsible for the convective heat transfer mechanisms, three different pipe lengths were investigated (3.69, 4.69 and 5.91 meters). In this manner both the flow pulsation frequency and the acoustic resonance modes of the pipe were varied, making it possible to study the influence of one characteristic on the other.

To characterize the acoustic resonance modes of the test-rig pipe for all the different lengths, a further experiment was conducted: after a thermal stabilisation of the experimental apparatus, by generating a steady hot air flow with an air temperature of 150°C at the inlet of the test section, the system was subjected to a pressure impulse and then allowed to resonate. Instantaneous pressures were measured at four different axial positions along the pipe and analysed to compute the resonance mode frequencies of the system.

4. Analytical Formulation of the Problem

As previously mentioned, the effect of the pulsation on heat transfers can be characterized in terms of the relative Nusselt number Nu_{rel} , defined as the ratio of the time-averaged Nusselt number for the pulsating flow to the corresponding one for a steady flow with the same time-averaged Reynolds number. For a cylindrical control volume, the time-averaged Nusselt number is defined as in the following equation:

$$Nu = \frac{hD}{\lambda} = \frac{Q_{conv}D}{S\Delta T_{lm}\lambda} \quad (1)$$

where: Q_{conv} is the time-averaged convective heat transfer, D the internal diameter of the pipe, S the exchange surface, ΔT_{lm} the logarithmic mean temperature difference between the air and the internal wall of the pipe and λ the thermal conductivity of air.

The relative Nusselt number definition has been adopted in several previous studies because of its ability to bring out the impact of the pulsation frequency on heat transfers and to identify a corrective coefficient for a Nusselt correlation accounting for pulsating effects. The practical difficulty in such an approach consists in correctly assessing the time-averaged convective heat transfer Q_{conv} . Since in some applications the measurement of the heat flux

exchanged with a solid wall is difficult to achieve, Q_{conv} is computed starting from the air flow properties by solving the energy balance equation.

The time-averaged convective heat transfer is generally computed from the variation of the time-averaged component of the air enthalpy through the inlet and outlet sections of the control volume, but it is shown in the following development that this calculation does not take into account characteristic terms related to the pulsating component of the flow. In the present work, Q_{conv} is derived from the time-averaged and space-integrated form of the instantaneous energy balance equation for a pulsating turbulent pipe flow. The terms related to the heat flux propagated from the advection of the oscillating component of the flow are highlighted.

Assuming negligible viscous dissipation, the 1D instantaneous local energy balance equation for an incompressible pipe flow with constant fluid properties exhibits the following form:

$$\rho c_p \left(\frac{\partial T}{\partial t} + \frac{\partial (uT)}{\partial x} \right) = \lambda \frac{\partial^2 T}{\partial x^2} + q \quad (2)$$

where u represents the bulk axial instantaneous air velocity, T the bulk temperature of air, ρ the fluid density, c_p the specific heat at constant pressure and q the local specific convective heat transfer exchanged through the perimeter of a pipe of length δx .

As proposed by Reynolds et al. [19], in the specific case of a turbulent pulsating flow, each of the flow properties can be decomposed into three different terms, as expressed in the following equation:

$$Z(t, x) = \bar{Z}(x) + \tilde{Z}(t, x) + Z'(t, x) \quad (3)$$

where $\bar{Z}(x)$ represents the time-averaged component only function of the x -axis, $\tilde{Z}(t, x)$ is the oscillating term of the coherent cycle-stationary pattern and $Z'(t, x)$ corresponds to the turbulent fluctuations term.

Time averaging ($\bar{}$) determines $\bar{Z}(x)$ and the *phase-average* ($\langle \rangle$), i.e. the average over a large ensemble of points having the same phase with respect to a reference oscillator, leads to:

$$\langle Z(t, x) \rangle = \bar{Z}(x) + \tilde{Z}(t, x) \quad (4)$$

Phase-averaging removes the background turbulence and extracts only the organized motions from the total

instantaneous profile. For the sake of brevity, some useful mathematical properties that follow from the basic definitions of the time and phase averages are not reported here. They are detailed in [19].

Combining Eq.3 and Eq.2 and then applying the phase averaging operator to the equation obtained leads to:

$$\begin{aligned} \rho c_p \left(\frac{\partial \bar{T}}{\partial t} + \frac{\partial \tilde{T}}{\partial t} + \frac{\partial (\bar{u}\bar{T})}{\partial x} + \frac{\partial (\tilde{u}\tilde{T})}{\partial x} + \frac{\partial (\bar{u}\tilde{T})}{\partial x} \right. \\ \left. + \frac{\partial (\tilde{u}\bar{T})}{\partial x} + \langle \frac{\partial (u'T')}{\partial x} \rangle \right) \\ = \lambda \left(\frac{\partial^2 \bar{T}}{\partial x^2} + \frac{\partial^2 \tilde{T}}{\partial x^2} \right) + \langle q \rangle \end{aligned} \quad (5)$$

In the left-hand side of this equation, the sum of the first two terms represents the rate of change of the air energy inside the control volume ($\frac{\partial \bar{T}}{\partial t}$ is equal to zero because of the time-independency of the component \bar{T}); the other terms represent the advective transport of energy by mean flow, oscillating motion and fluctuating motion through the control volume. In the right-hand side of the equation, the sum of the first two terms corresponds to the conduction heat flux through the control volume and the last term represents the phase-average of the local convective heat transfer between the air and the solid wall. Time-averaging Eq. 5 leads to:

$$\begin{aligned} \rho c_p \left(\frac{\partial (\bar{u}\bar{T})}{\partial x} + \frac{\partial (\tilde{u}\tilde{T})}{\partial x} + \frac{\partial \langle (u'T') \rangle}{\partial x} \right) \\ = \lambda \left(\frac{\partial^2 \bar{T}}{\partial x^2} \right) + \langle q \rangle \end{aligned} \quad (6)$$

By integrating Eq. 6 on the volume defined by a cylinder of section ' S ' and length ' L ' (corresponding to the control volume, between the inlet and outlet measuring sections, in the following), the energy conservation equation can be written as:

$$\begin{aligned} \rho c_p S \left(\underbrace{\bar{u}\bar{T}|_0^L}_A + \underbrace{\tilde{u}\tilde{T}|_0^L}_B + \underbrace{\langle u'T' \rangle|_0^L}_C \right) \\ = \int_V \langle q(x, t) \rangle dV = Q_{conv} \end{aligned} \quad (7)$$

The total time-averaged convective heat transfer Q_{conv} is equal to the sum of three different terms: the term 'A' which physically represents the energy variation of the time-mean component of the flow across the pipe, the term 'B' which represents the energy variation due to the oscillating component of the flow and the term 'C' corresponding to the advective transport of energy by fluctuating motion due to turbulence fluctuations. The statement of Eq. 7 clarifies that, whenever a direct measurement of Q_{conv} is not available, instantaneous measurements of the air velocity and temperature are required to correctly compute all the terms in the left-hand side of Eq. 7. In this study, as previously presented, a water flow was used to cool the external surface of the pipe. In addition to keeping the wall temperature cold, constant and quite homogeneous in the pipe section where heat transfers are characterized, this experimental setup allows Q_{conv} to be evaluated directly from the water temperature measurements. In this manner, it is possible to avoid performing instantaneous measurements of the flow properties at the inlet and the outlet of the test-section.

5. Results and Discussion

5.1. Acoustic Characterization of the Pipe

When the experimental apparatus is excited with an impulsive pressure source, the resonance frequencies of the system can be calculated by computing the power spectral density (PSD) of the pressure signal. These frequencies correspond to the local maxima of the PSD. In this study, a second order low-pass filter with a cut-off frequency of 1 kHz was applied to the sensor signals before calculating the PSD. Sensor signals were acquired at a frequency of 20 kHz, high enough to respect the Nyquist-Shannon sampling theorem. Because the behaviour of the pressure response to the impulsive pressure excitation is qualitatively the same for each pipe length, in the following figures only the pressure signal for one pipe length is shown. Figure 3 shows the instantaneous pressure, measured at the centre of the test-section, and figure 4 shows the PSD of the signal obtained for a specific pipe length. The other pressures, measured at different pipe axial positions or for the other pipe lengths, show the same PSD results and are not reported here. Local maxima of the PSD, identified by the red points on figure 4, correspond to the resonance frequencies of the system. Table 1 shows the first six

calculated resonance frequencies for the three pipe lengths tested.

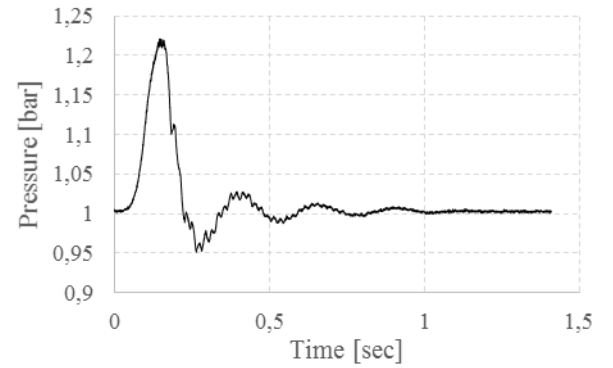


Figure 3. Instantaneous pressure, $L = 5.91\text{m}$.

Results show that the first resonance mode of the system is quite different from the resonance frequency calculated for a pipe closed at one end and open to the surrounding air at the other end, which is equal to $f_r = \frac{nc}{4L}$, where n is a natural integer number equal to 1 for the first resonance mode, c is the sound speed and L is the pipe length. This means that the volume of the outlet plenum is not large enough to be representative of an open exhaust at pressure and temperature ambient conditions. This implies that a detailed numerical modeling of the experimental apparatus should take into account this result through the description of the boundary conditions.

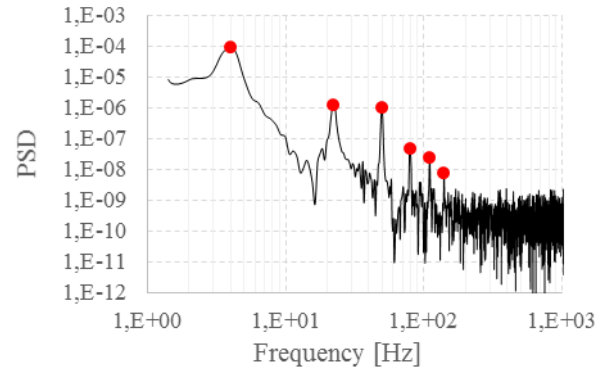


Figure 4. Power Spectral Density, $L = 5.91\text{m}$.

Table 1. Resonance frequencies [Hz] of the test-bench for different pipe lengths.

Resonance Modes	1	2	3	4	5	6
$L = 3.69\text{m}$	6.4	36.1	79.6	126.3	176.2	239.8
$L = 4.69\text{m}$	4.7	26.2	63.1	101.3	138.9	175.8
$L = 5.91\text{m}$	3.9	22.2	49.5	80.5	110	139.8

5.2. Pulsation Effects on Convective Heat Transfers

As previously mentioned, given the difficulty of measuring the three terms in the left-hand side of Eq. 7 experimentally, the total time-averaged convective heat transfer Q_{conv} was evaluated from the water temperature measurements. In practice, a constant water volumetric flow rate of $4.74 \text{ dm}^3/\text{min}$ is forced to pass through an annular section, with an internal diameter of 67.3 mm and a thickness of 7 mm , in order to cool the pipe wall. In these operating conditions, the Reynolds number of the water flow is 788 , leading to a laminar velocity profile under steady state conditions. Consequently, from the energy balance equation for the water, in which the convective heat transfer with the exterior ambient air was estimated to be less than 10 W and was therefore neglected, Q_{conv} can be solved as the time-averaged enthalpy difference of the water between the inlet and the outlet of the test-section.

The air steady turbulent state (for the particular case with a time-averaged Reynolds number of 30000) is taken as the reference case. In such particular conditions, the term 'B' in Eq. 7 is null, making it possible to compare Q_{conv} computed from experiments to the theoretical predicted one. The Nusselt number was evaluated using the Colburn and the Dittus-Boelter correlations and applying the Bhatti and Shah corrective coefficient [20] to take entry effects into account. For a Re of 30000 , the space-averaged Nusselt number was found to be equal to 89.4 with the Colburn correlation and 92 with the Dittus-Boelter correlation. The total convective heat transfer linked to the Colburn correlation is 482 W , which corresponds to a difference of 2.7% with the experimental value. With the Nusselt number calculated from the Dittus-Boelter correlation the agreement is even better, with a difference of less than 1% . Consequently, the small differences between the theoretical predictions and the experiment validate the evaluation of the total convective heat transfer based on water temperature measurements.

A further comparison between Q_{conv} and term 'A' in Eq. 7, in the case of the steady turbulent flow, shows that the calculation of the variation in the time-averaged enthalpy of air is not sufficient to correctly compute the total time-averaged convective heat transfer: not taking into account the turbulent term may lead to an underestimation of the total time-averaged convective heat transfer of around 22% . The term 'A' was computed by calculating the bulk flow temperature at the test-section inlet and outlet.

Figure 5 shows the term Q_{conv} of Eq. 7 for different time-averaged Reynolds numbers, evaluated at the pipe length of 5.91 m .

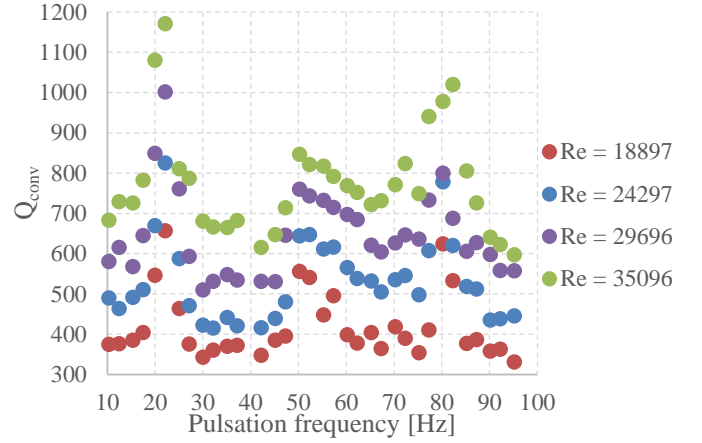


Figure 5. Q_{conv} for different time-averaged Reynolds numbers and pulsation frequencies.

Results show that an increase in the time-averaged Reynolds number leads to an increase in the convective heat transfers, as could easily be deduced from a Nusselt correlation for a stationary turbulent flow. However, for particular excitation frequencies a strong heat transfer improvement occurs for all the tested mass flow rates, suggesting that the mechanism leading to this heat transfer enhancement is independent of the Reynolds number.

In order to understand this mechanism, the time-averaged Nusselt number $Nu = \frac{h_{air}D}{\lambda}$ was calculated in the particular case of a $Re = 29696$. It was evaluated by modelling the heat transfer between the hot air and the water with three thermal resistances placed in series to describe the internal forced convection of the air, the radial conduction through the wall and the forced convection of the water.

The air convective heat transfer coefficient h_{air} assumes the following form:

$$h_{air} = \frac{\left(\frac{Q_{conv}}{\Delta T_{lm}} - \frac{\ln\left(\frac{R_{out}}{R_{in}}\right)}{2\pi L \lambda_{wall}} - \frac{1}{h_{water} 2\pi R_{out} L} \right)}{2\pi R_{in} L} \quad (8)$$

where R_{out} and R_{in} are the inner and outer diameters of the annular section of the water, L is the length of the test-section, λ_{wall} is the thermal conductivity of the wall, ΔT_{lm} is the logarithmic temperature difference

usually used in the case of heat exchangers and h_{water} is the convective heat transfer coefficient of the water. The latter was calculated according to the work of Dirker et al. [21], and ΔT_{lm} was calculated according to the following equation:

$$\Delta T_{lm} = \frac{(T_{b_{in}} - T_{H2O-in}) - (T_{b_{out}} - T_{H2O-out})}{\ln\left(\frac{(T_{b_{in}} - T_{H2O-in})}{(T_{b_{out}} - T_{H2O-out})}\right)} \quad (9)$$

The relative time-averaged Nusselt number (defined as the ratio of the time-averaged Nusselt number for the pulsating flow to the corresponding one for a steady flow with the same time-averaged Reynolds number), Nu_{rel} , is reported on figure 6 as a function of the Womersley number for the experiment corresponding to $Re=29696$ and for all the tested frequency range. Uncertainties are depicted by error bars in the figure. The Womersley number, defined as $Wo = \frac{L}{2} \sqrt{\frac{\rho\omega}{\mu}}$, which is a ratio of the channel height to the Stokes boundary-layer thickness, is a dimensionless expression of the pulsatile flow frequency in relation to viscous effects. L represents the characteristic length of the system and for a pipe flow is equal to the pipe internal diameter. The condition of no-slip at the wall necessitates that for a pulsating flow, in order to accommodate the imposed variation of flow rate additional vorticity must be generated in the boundary layer in a manner which varies with time. Thus coherent shear waves are excited which propagate from the wall into the fluid and are attenuated within a penetration length. In the case of laminar pulsating flow, as claimed from Uchida [22] the wave attenuation is characterized by a length scale $k = \sqrt{\frac{\nu}{\omega}}$ (in which ν is the kinematic viscosity of the fluid and ω is the angular frequency of the pulsation). This length scale is usually referred to as the Stokes layer thickness in recognition of the pioneering contribution which Stokes made to the theory of unsteady flow.

Results show that for the entire Womersley range the relative time-averaged Nusselt number is always greater than 1: flow pulsation has a positive effect on heat transfers so that an enhancement of the internal forced convection, in comparison to the steady flow, is observed. This behaviour was found to be independent of the Reynolds number. According to the definitions of

the Womersley number and of the Stokes layer, an increase of the pulsation frequency leads to a thinning of the viscous fluid boundary layer for the pulsating flow, which means that the velocity field is affected in a more restricted zone near the wall with the increase of Wo . However, in terms of heat transfer enhancement, local optimal values of the Womersley number exist for the maximization of the relative Nusselt number. This result indicates that the transport of energy and the transport of the momentum are differently impacted by the variation of the Womersley number. This result agrees with the experimental results in Ref. [11], where a local maximum in the heat transfer enhancement was found for a particular value of Wo . In the present study, these optimal values of Wo , where a local maximum of the relative time-averaged Nusselt number appears, correspond to pulsation frequencies identified as resonance frequencies of the system (that are 22.5, 50 and 80 Hz). Similar results were found by varying the pipe length for this time-averaged Reynolds number: for each of the pipe lengths tested when the flow is excited, with a pulsation frequency equal to one of the resonance modes, a heat transfer enhancement occurs. However, the magnitude of the heat transfer enhancement differs for each resonance mode and pipe length. This kind of result suggests that a coherent heat transfer enhancement mechanism exists when the flow is in resonant state.

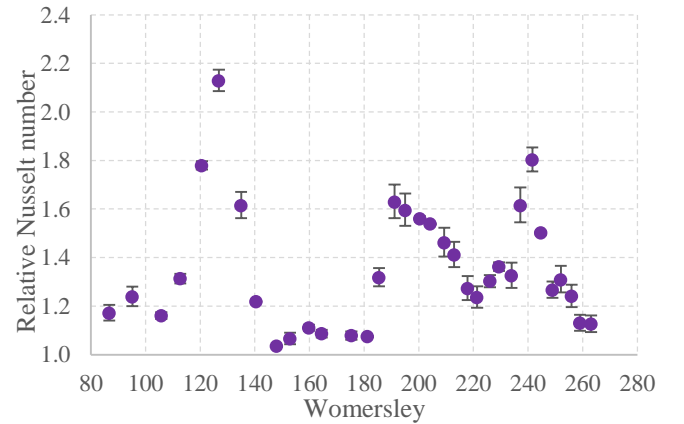


Figure 6. Relative time-averaged Nusselt number for $Re=29696$.

To describe this mechanism, the instantaneous radial profile measurements of air velocity and temperature at the middle of the test-section (section B – B' in Fig. 4) were analysed. Using the 1D assumption adopted, it is possible to calculate the local terms in the left side of Eq. 6. In order to be in agreement with the

1D approach, the physical quantities correspond to the integral of the measured profiles on the cross section.

Instantaneous measurements were conducted only for pulsation frequencies below 30 Hz since the size of the thermocouple means that measurements for higher frequencies cannot be exploited due to the time constant of the thermocouple that cannot be compensated using a Kalman filter method. The measurement procedure of the instantaneous profiles of air axial velocity, using hot-wire anemometry, and air temperature, with micro unsheathed thermocouples, requires a correction of the hot-wire signals to account for the temperature variation of air as well as a thermocouple signal compensation for the sensor time delay. For frequencies higher than 30 Hz, the implicit filtering of the real temperature variations, due to the thermal inertia of the sensors, makes compensation of the thermocouple signal unfeasible, nor does it allow temperature compensation of the hot-wire signal. The pulsation frequencies below 30 Hz were chosen as a function of particular heat transfer conditions: 10 Hz and 12.5 Hz were selected for the light impact on heat transfers, 20 Hz and 22.5 Hz because of their vicinity to the second resonance mode of the pipe, and 30 Hz because it has the smallest relative Nusselt number.

The term $\bar{u}\bar{T}$, which represents the enthalpy transported by the time-averaged component of the flow, was found to be slightly dependent on the pulsation frequency.

The term $\overline{(u'T')}$ could not be computed from the experimental results because of the impossibility of measuring the turbulent components of the flow velocity and temperature. However, assuming that the variation in the pulsation frequency does not significantly impact the turbulence properties, it can be considered that this term will not modify the convective heat transfer when the pulsation frequency is changed.

Since the Peclet number, defined as the ratio of the advection and diffusion rates of the thermal energy and equal to the product of the Nusselt and Prandtl numbers, is much higher than 1 in the present experimental conditions, heat transfers occur in a convective dominant regime and hence, the conduction term in Eq. 6 can be neglected.

Finally, the results for the terms $\bar{u}\bar{T}$ and $\frac{\Delta\langle u \rangle}{\bar{u}}$ are reported in the following figures (Fig. 7 & Fig. 8). $\frac{\Delta\langle u \rangle}{\bar{u}}$ represents the weight of the phase-averaged velocity oscillation amplitude on the time-averaged velocity

component and characterizes the increase in the oscillating component of the flow due to pulsation.

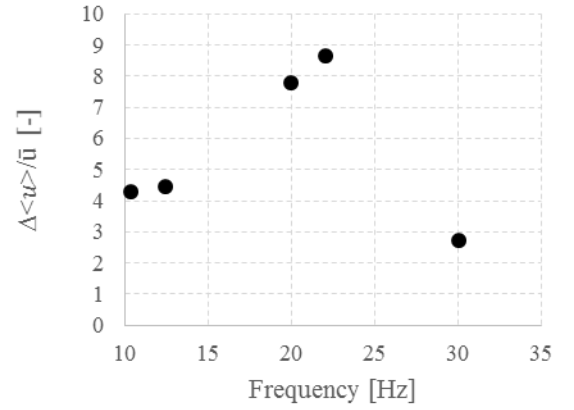


Figure 7. $\frac{\Delta\langle u \rangle}{\bar{u}}$ as a function of the pulsation frequency.

The results in figure 7 show a maximum of the term $\frac{\Delta\langle u \rangle}{\bar{u}}$ corresponding to the resonance frequency of the system, indicating that a flow resonance implies a wide oscillating velocity component. Furthermore, since $\frac{\Delta\langle u \rangle}{\bar{u}}$ values are all higher than 1, it can be concluded that flow reversal occurs for all the frequencies analysed in figure 7, as confirmed by the instantaneous measurements of the air velocity with the double wire probe.

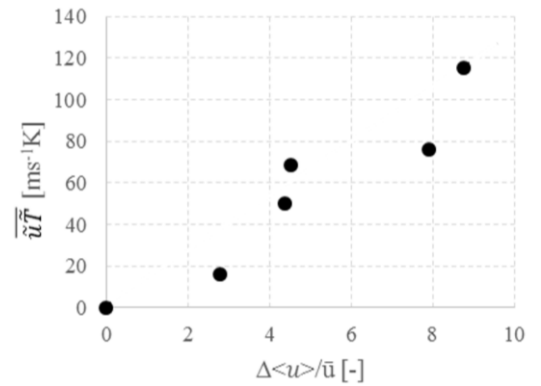


Figure 8. $\bar{u}\bar{T}$ as a function of $\frac{\Delta\langle u \rangle}{\bar{u}}$.

The results in figure 8 show the term $\bar{u}\bar{T}$ as a function of $\frac{\Delta\langle u \rangle}{\bar{u}}$. By linking figures 7 and 8, it can be observed that large velocity oscillations, which correspond to high $\frac{\Delta\langle u \rangle}{\bar{u}}$ values, are favoured for pulsation frequencies close to the resonance frequency

(the highest values of $\frac{\Delta\langle u \rangle}{\bar{u}}$ correspond to the frequencies around the second resonance mode of the system, i.e. 22.5 Hz) and lead to an increase of $\overline{\tilde{u}\tilde{T}}$ as a function of $\frac{\Delta\langle u \rangle}{\bar{u}}$. The linear trend that seems to emerge in figure 8 cannot be asserted because of the frequency domain in which temperature and air velocity measurements have been conducted is too narrow. The heat transfer enhancement for these frequencies, observed on figure 6, is therefore mainly attributed to a large oscillating component of the fluid velocity which increases the oscillating heat advection.

5. Conclusion

In this study, the heat transfer mechanism for a pulsating turbulent pipe flow has been investigated. A test-rig, designed to generate a pulsating hot air flow representative of the intake and exhaust of an internal combustion engine, has been presented, in which a pulsating turbulent hot air flow exchanges energy with a water cooled pipe with a pulsation frequency ranging from 10 to 95 Hz and a Reynolds number, based on the time-averaged velocity, ranging from 1.8×10^4 to 3.5×10^4 . Three different pipe lengths were investigated.

Particular attention was paid to the calculation of the time-averaged convective heat transfer by developing an analytical formulation of the heat transfer problem for a 1D pulsating turbulent pipe flow. This development evidenced that whenever a direct measurement of the total time-averaged convective heat transfer is not available, instantaneous measurements of the air velocity and temperature are required to correctly compute the terms linked to the oscillating component of the flow in the energy balance equation.

Experimental results showed that the flow pulsation enhances heat transfers in the entire range of frequencies investigated for all the Reynolds numbers tested. Furthermore, for particular pulsation frequencies, the heat transfer improvement due to pulsation is higher than the heat transfer enhancement that can be achieved with a Reynolds number increase. In particular, it was experimentally observed that, when the flow is excited with a frequency equal to a resonance mode of the system, a strong increase in heat transfers occurs. Instantaneous measurements of air velocity and temperature demonstrated that the increase in the energy axial advection due to the oscillating component of the velocity is the major cause of the heat transfer enhancement. This behaviour was

observed to be independent of the pipe length, and therefore independent of the acoustic resonance modes of the pipe. These results suggest that flow pulsation may be used as an active method for heat transfer enhancement.

In addition to the results presented in this paper, a radial transport enhancement of thermal energy during flow reversal was observed and will be studied and characterized with a 2D approach in future work.

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